

General Certificate of Education

Mathematics 6360

MS04 Statistics 4

Mark Scheme

2006 examination - June series

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation meeting attended by all examiners and is the scheme which was used by them in this examination. The standardisation meeting ensures that the mark scheme covers the candidates' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for the standardisation meeting each examiner analyses a number of candidates' scripts: alternative answers not already covered by the mark scheme are discussed at the meeting and legislated for. If, after this meeting, examiners encounter unusual answers which have not been discussed at the meeting they are required to refer these to the Principal Examiner.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of candidates' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

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Key To Mark Scheme And Abbreviations Used In Marking

M	mark is for method			
m or dM	mark is dependent on one or more M marks and is for method			
A	mark is dependent on M or m marks and is for accuracy			
В	mark is independent of M or m marks and is for method and accuracy			
Е	mark is for explanation			
√or ft or F	follow through from previous			
	incorrect result	MC	mis-copy	
CAO	correct answer only	MR	mis-read	
CSO	correct solution only	RA	required accuracy	
AWFW	anything which falls within	FW	further work	
AWRT	anything which rounds to	ISW	ignore subsequent work	
ACF	any correct form	FIW	from incorrect work	
AG	answer given	BOD	given benefit of doubt	
SC	special case	WR	work replaced by candidate	
OE	or equivalent	FB	formulae book	
A2,1	2 or 1 (or 0) accuracy marks	NOS	not on scheme	
–x EE	deduct x marks for each error	G	graph	
NMS	no method shown	c	candidate	
PI	possibly implied	sf	significant figure(s)	
SCA	substantially correct approach	dp	decimal place(s)	

No Method Shown

Where the question specifically requires a particular method to be used, we must usually see evidence of use of this method for any marks to be awarded. However, there are situations in some units where part marks would be appropriate, particularly when similar techniques are involved. Your Principal Examiner will alert you to these and details will be provided on the mark scheme.

Where the answer can be reasonably obtained without showing working and it is very unlikely that the correct answer can be obtained by using an incorrect method, we must award **full marks**. However, the obvious penalty to candidates showing no working is that incorrect answers, however close, earn **no marks**.

Where a question asks the candidate to state or write down a result, no method need be shown for full marks.

Where the permitted calculator has functions which reasonably allow the solution of the question directly, the correct answer without working earns **full marks**, unless it is given to less than the degree of accuracy accepted in the mark scheme, when it gains **no marks**.

Otherwise we require evidence of a correct method for any marks to be awarded.

			AQA	GCE Mark Scheme, 2006 June series Comments Or S^2 or $(n-1)S^2 = 764.875$
S04				SCIOUS
Q Q	Solution	Marks	Total	Comments
1(a)	S = 10.45	B1		Or S^2 or $(n-1)S^2 = 764.875$
	v = 7	B1	1	
	$\chi^2_7(0.025) = 1.690$			
	$\chi^2_7(0.975) = 16.013$	B1		Both
	95% confidence limits for σ^2 are			
	$\frac{7 \times 10.45^2}{16.013}$ and $\frac{7 \times 10.45^2}{1.690}$	M1 A1√		ft on S^2 and χ^2
	95% CI for σ^2 is		1	
	(47.8, 453)	A1	6	AWRT
(b)	6 ² ∉ CI	E1√	1	or $6 < \sqrt{47.8}$
	Reject $\sigma = 6$	E1	2	CAO
	Total	 	8	
2(a)	H ₀ : accept binomial distribution	B1	1	
	E_i ratio 1:3:3:1	M1	1	
	⇒30:90:90:30	A1		
	$\sum \left\{ \frac{\left(O_i - E_i\right)^2}{E_i} \right\} = \frac{36}{30} + \frac{36}{90} + \frac{49}{90} + \frac{25}{30}$	M1		
	= 2.98	A1		Accept 2.96 to 2.99
	v = 4 - 1 = 3, c.v. = 7.815	B1, B1		
	Accept this is $B\left(3,\frac{1}{2}\right)$	A1	8	CSO
(b)(i)	Calculate mean ÷3	E1 E1	2	May use numbers from question
(ii)	2	B1	1	
	Total		11	

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MS04 (cont)		3.5 -	7F	
Q	Solution	Marks	Total	Comments
3(a)(i)	$\left[-e^{-0.2x}\right]_0^2$	M1		
	$=1-e^{-0.4}=0.330$	A1	2	AWRT (Accept 0.33)
(ii)	$=1 - e^{-0.4} = 0.330$ $1 - \left[-e^{-0.2x} \right]_0^3$	M1		
	$=e^{-0.6}=0.549$	A1	2	AWRT
(b)(i)	$E(X) = \int_0^\infty \lambda x e^{-\lambda x} dx$	M1		Limits Required
	$= \left[-xe^{-\lambda x} \right]_0^{\infty} + \int_0^{\infty} e^{-\lambda x} dx$	A1		
	$= \left[0\right] - \left[0\right] + \left[\frac{-e^{-\lambda x}}{\lambda}\right]_0^{\infty}$	A1		
	$= 0 - \left[-\frac{1}{\lambda} \right]$ $= \frac{1}{\lambda}$	A1	4	
(ii)	$\int_{0}^{m} \lambda e^{-\lambda x} dx = \frac{1}{2}$ $\Rightarrow \left[-e^{-\lambda x} \right]_{0}^{m} = \frac{1}{2}$	M1		Must use integration, not quote cdf
	$\Rightarrow \left[-e^{-\lambda x} \right]_0^m = \frac{1}{2}$			
	$\Rightarrow 1 - e^{-\lambda m} = \frac{1}{2}$			
	$\Rightarrow e^{\lambda m} = 2$	m1		Dependent on previous M
	$\Rightarrow m = \frac{1}{\lambda} \ln 2$	A1	3	OE, eg $\frac{-\ln 0.5}{\lambda}$ or $\frac{0.693}{\lambda}$
(c)(i)	$\frac{1}{0.3} \times 24 = 80 \text{ hours}$	B1	1	
	$\frac{1}{0.3} \ln 2 \times 24 = 80 \ln 2 \text{ hours}$	M1 A1	2	Or 55.5 hours AWRT
				M1 for 2.31 (days)
	Total		14	

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MS04 (cont)				
Q	Solution	Marks	Total	Comments
5(a)	$E(aX+bY)=\mu$			
	$\Rightarrow aE(X) + bE(Y) = \mu$	M1		
	$\Rightarrow aE(X) + bE(Y) = \mu$ $\Rightarrow 2\mu a + \mu b = \mu$ $\Rightarrow 2a + b = 1$			
	$\Rightarrow 2a + b = 1$	A1	2	AG (working required)
(b)	$\operatorname{Var}(aX + bY) = a^2 \operatorname{Var}(X) + b^2 \operatorname{Var}(Y)$			
	$=13a^2+3b^2$	M1		
	$=13a^2 + 3(1-2a)^2$	M1		
	$= 13a^2 + 3 - 12a + 12a^2$			
	$= 3 - 12a + 25a^2$	A1	3	AG (working required)
(c)	$\frac{\mathrm{d}V}{\mathrm{d}a} = 0 \text{ for min } V$			
	$\Rightarrow -12a + 50a = 0$	M1		
	$\Rightarrow a = \frac{12}{50} = 0.24$	A1		
	b = 1 - 0.48 = 0.52	A1	3	
(d)	$\mu = 15 \times 0.24 + 10 \times 0.52$	m1	2	Dependent on previous M
	= 8.8	A1	2	
	Total		10	

4 (cont)				GCE Mark Scheme, 2006 June series That have been series Course the Comments
Q	Solution	Marks	Total	Comments
6(a)(i)	$P(3) = 0.6^2 \times 0.4$	M1		
	= 0.144	A1	2	
(ii)	$P(>3) = 1 - 0.4(1 + 0.6 + 0.6^2)$	M1		
	or 0.6^3 = 0.216	A1	2	
		711	2	
(b)(i)	$E(X) = 1.p + 2qp + 3q^2p +$	M1		
	$= p\left(1 + 2q + 3q^2 + \ldots\right)$	A1		
	$E(X) = 1 \cdot p + 2qp + 3q^{2}p + \dots$ $= p(1 + 2q + 3q^{2} + \dots)$ $= p(1 - q)^{-2}$			
	$=\frac{p}{p^2}$			
	$\begin{vmatrix} P \\ = \frac{1}{-} \end{vmatrix}$			
	p	A1	3	AG (working required)
(ii)	$\operatorname{Var}(X) = \frac{2-p}{p^2} - \left(\frac{1}{p}\right)^2$ $= \frac{1-p}{p^2}$	M1		
	$=\frac{1-p}{p^2}$	A1	2	AG
(c)(i)	$0.2 + 0.8 \times 0.2 = 0.36$	B1	1	
(ii)	$E(Y) = \frac{1}{0.2} = 5$	B1		
	$Var(Y) = \frac{0.8}{0.04} = 20$	B1	2	
(iii)	$E(Y) = \frac{1}{0.2} = 5$ $Var(Y) = \frac{0.8}{0.04} = 20$ $\frac{\sqrt{20}}{\sqrt{5}} = 2$	B1		
	$P(Y \le 3) = 0.36 + 0.8^2 \times 0.2$	M1		Or $1 - (1 - p)^3 = 1 - 0.8^3$
	= 0.488	A1	3	Correct number of terms required for M1